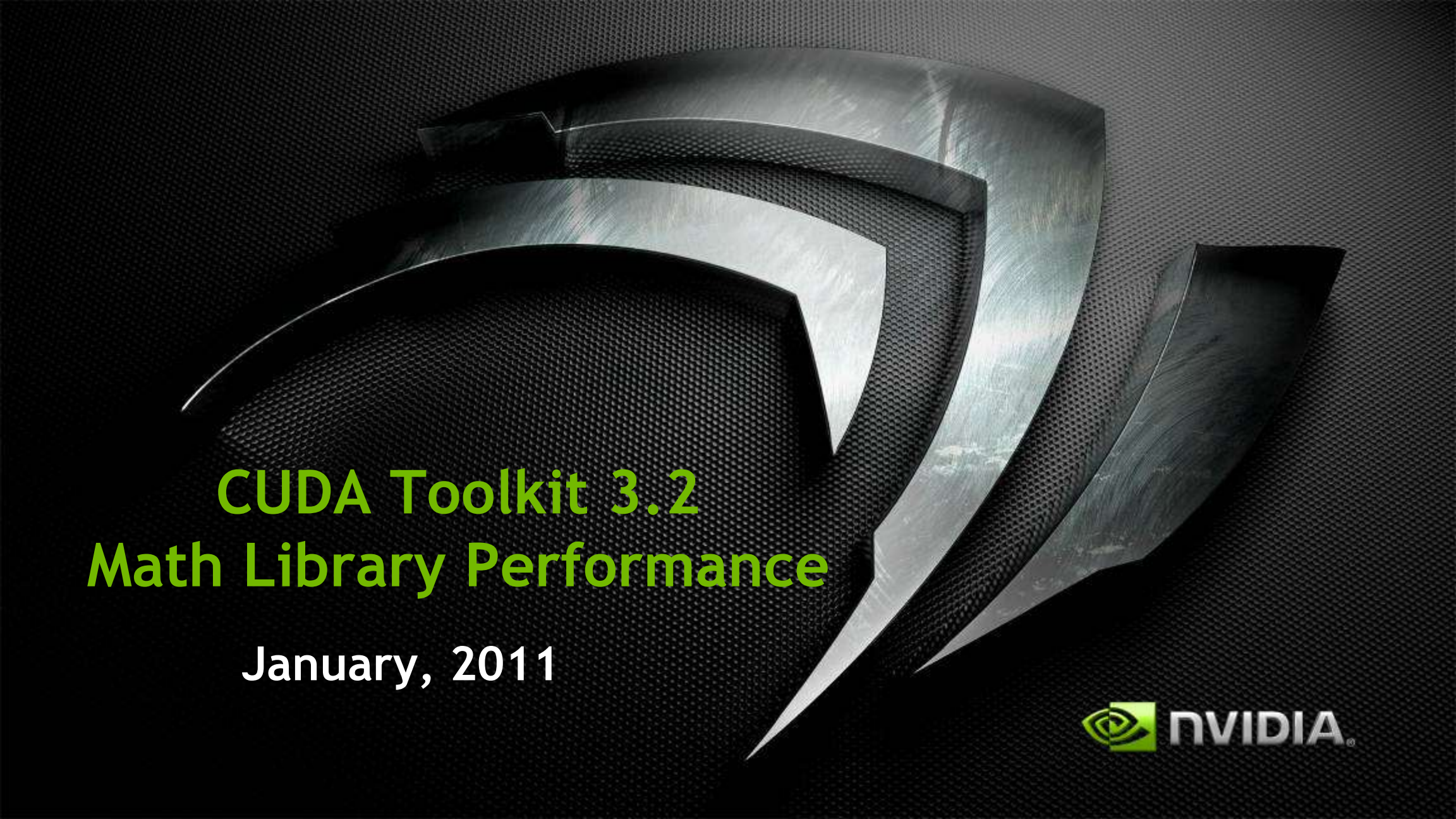


An abstract 3D graphic featuring several curved, metallic-looking bands that overlap and curve around each other, creating a sense of depth and motion. The bands have a brushed metal texture and are set against a dark, textured background.

CUDA Toolkit 3.2 Math Library Performance

January, 2011



CUDA Math Libraries

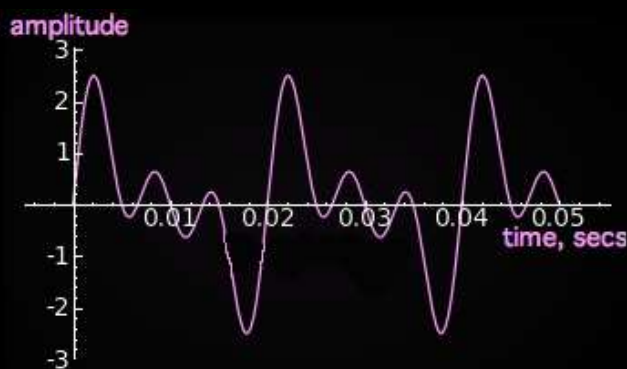
High performance math routines for your applications:

- cuFFT - Fast Fourier Transforms Library
- cuBLAS - Complete BLAS Library
- cuSPARSE - Sparse Matrix Library
- cuRAND - Random Number Generation (RNG) Library

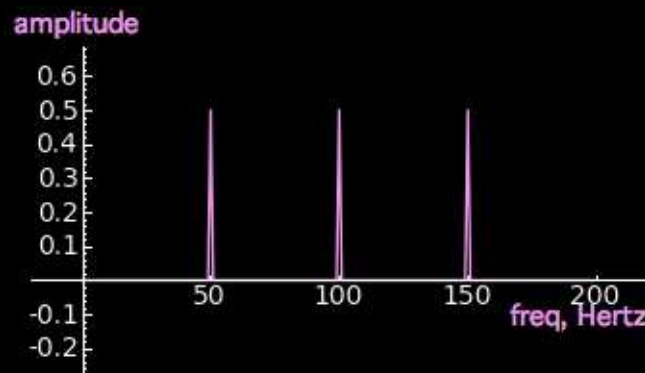
- Included in the CUDA Toolkit (free download)
 - www.nvidia.com/getcuda
- For more information on CUDA libraries:
 - <http://www.nvidia.com/object/gtc2010-presentation-archive.html#session2216>

cuFFT

- Multi-dimensional Fast Fourier Transforms
- New in CUDA 3.2:
 - Higher performance of 1D, 2D, 3D transforms with dimensions of powers of 2, 3, 5 or 7
 - Higher performance and accuracy for 1D transform sizes that contain large prime factors



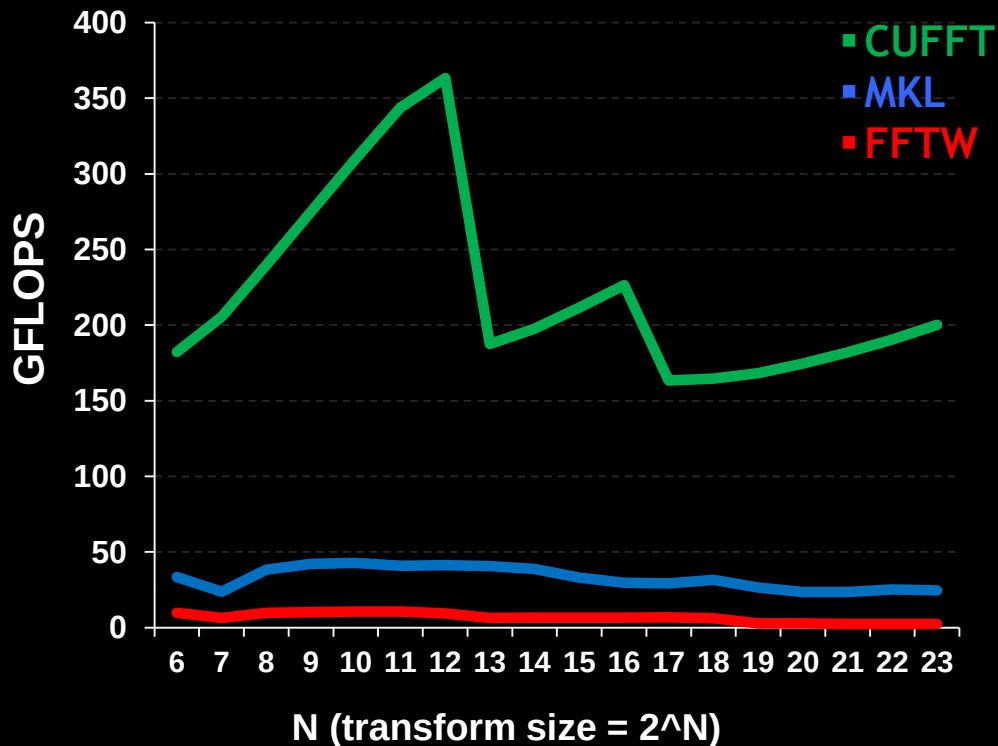
$$F(x) = \sum_{n=0}^{N-1} f(n) e^{-j2\pi(x\frac{n}{N})}$$
$$f(n) = \frac{1}{N} \sum_{x=0}^{N-1} F(x) e^{j2\pi(x\frac{n}{N})}$$



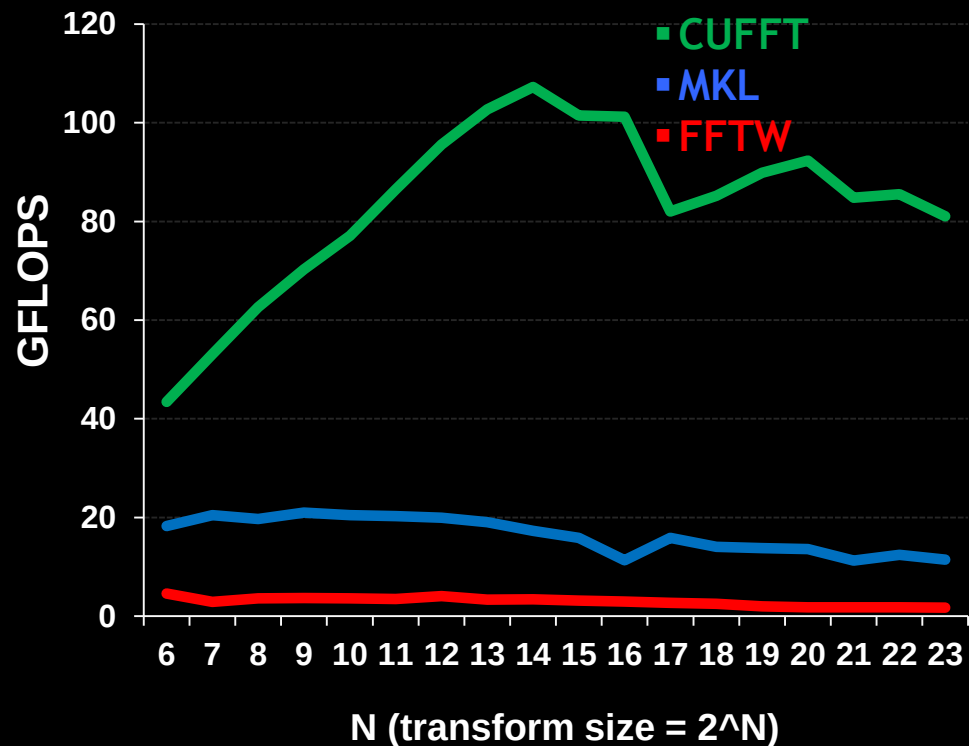
FFTs up to 8.8x Faster than MKL

1D used in audio processing and as a foundation for 2D and 3D FFTs

Single-Precision 1D Radix-2



Double-Precision 1D Radix-2

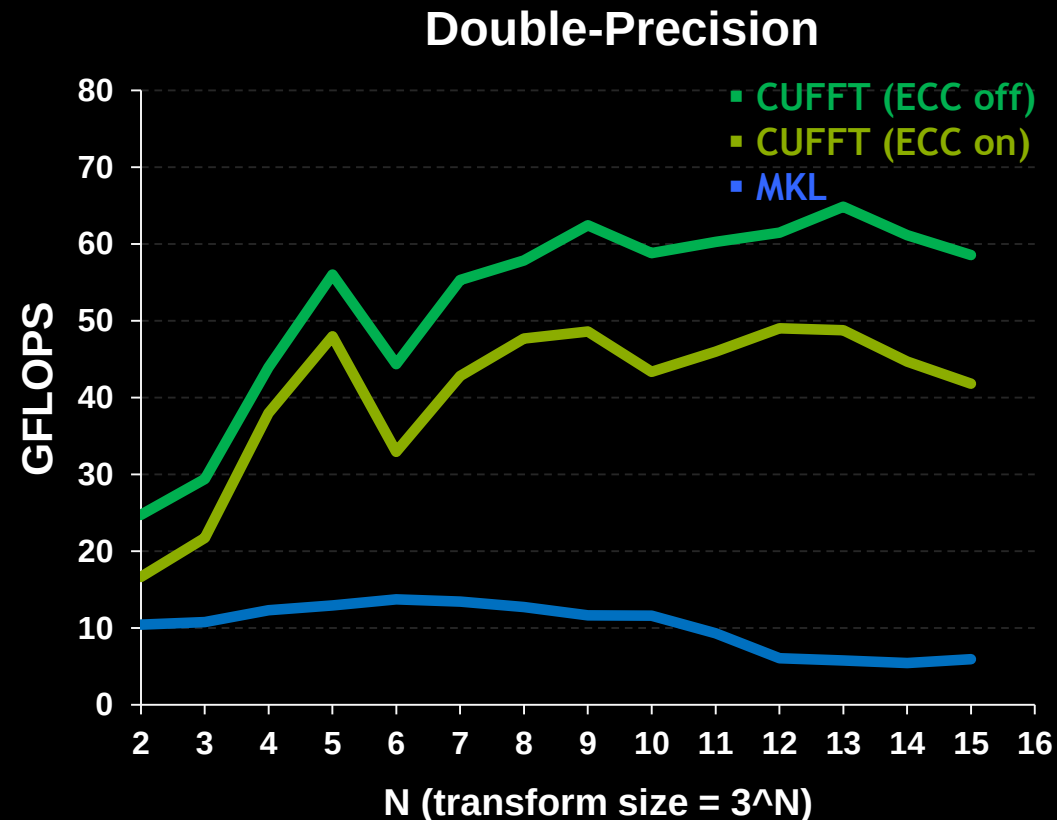
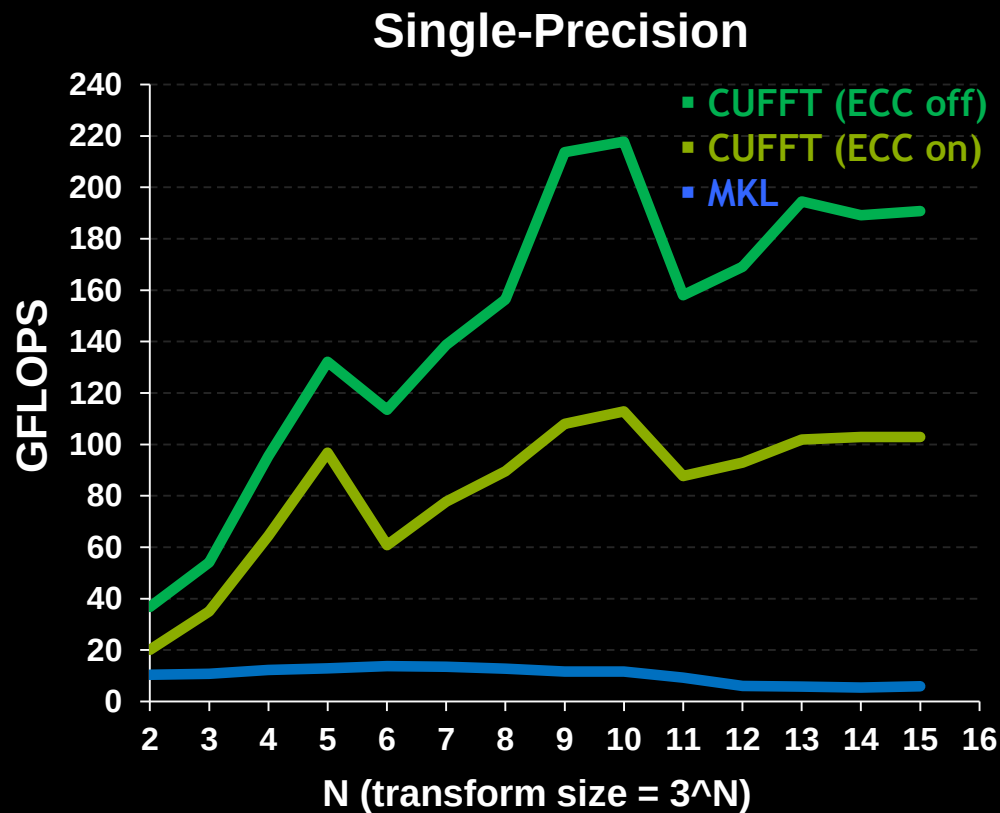


- * cuFFT 3.2, Tesla C2050 (Fermi) with ECC on
- * MKL 10.1r1, 4-core Corei7 Nehalem @ 3.07GHz
- * FFTW single-thread on same CPU

cuFFT 1D Radix-3 up to 18x Faster than MKL

18x for single-precision, 15x for double-precision

Similar acceleration for radix-5 and -7



* CUFFT 3.2 on Tesla C2050 (Fermi)

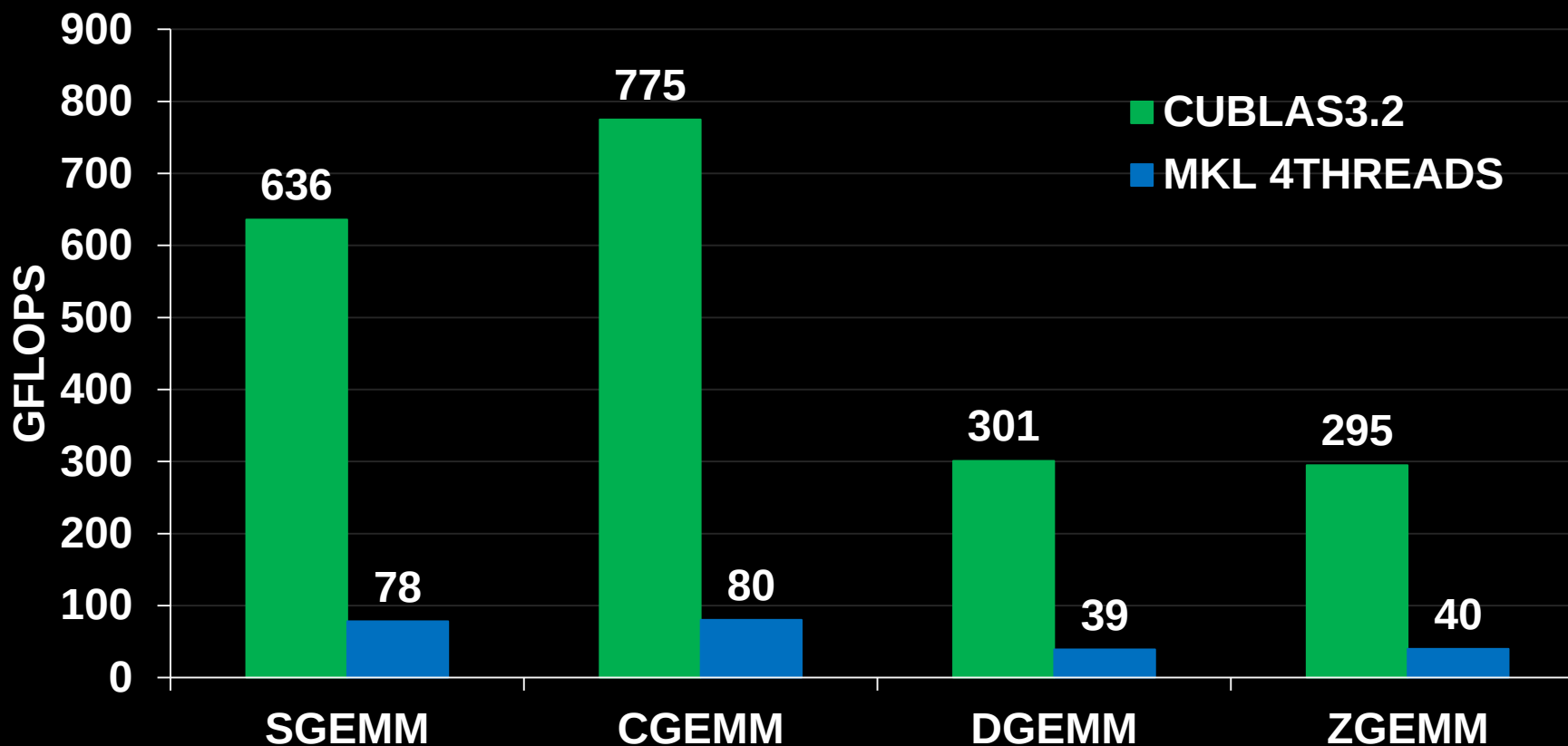
* MKL 10.1r1, 4-core Corei7 Nehalem @ 3.07GHz

cuBLAS: Dense Linear Algebra on GPUs

- Complete BLAS implementation
 - Supports all 152 routines for single, double, complex and double complex
- New in CUDA 3.2
 - 7x Faster GEMM (matrix multiply) on Fermi GPUs
 - Higher performance on SGEMM & DGEMM for all matrix sizes and all transpose cases (NN, TT, TN, NT)

Up to 8x Speedup for all GEMM Types

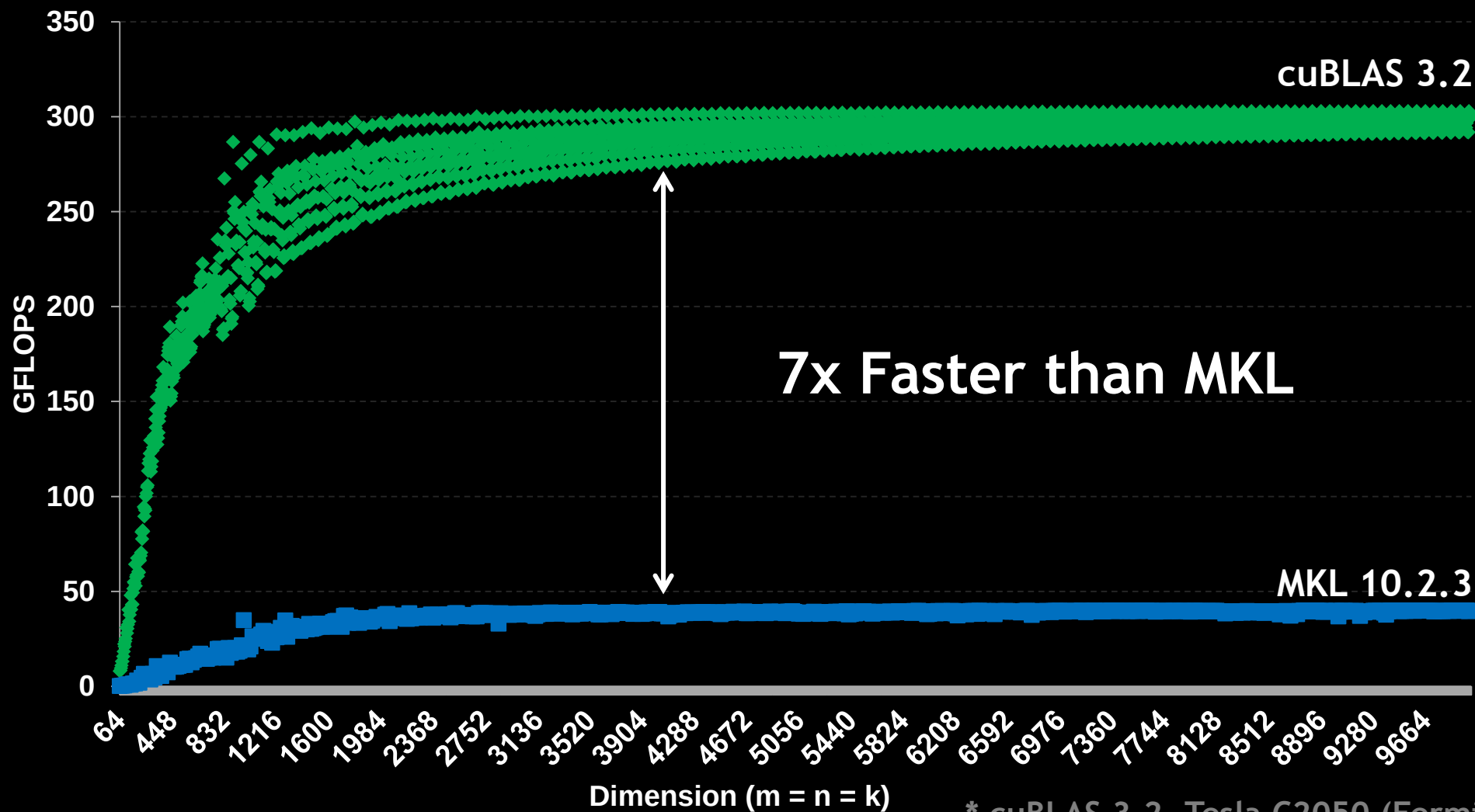
GEMM Performance on 4K by 4K matrices



* cuBLAS 3.2, Tesla C2050 (Fermi), ECC on

* MKL 10.2.3, 4-core Corei7 @ 2.66Ghz

7x Faster DGEMM Performance



* cuBLAS 3.2, Tesla C2050 (Fermi), ECC on

* MKL 10.2.3, 4-core Corei7 @ 2.66Ghz

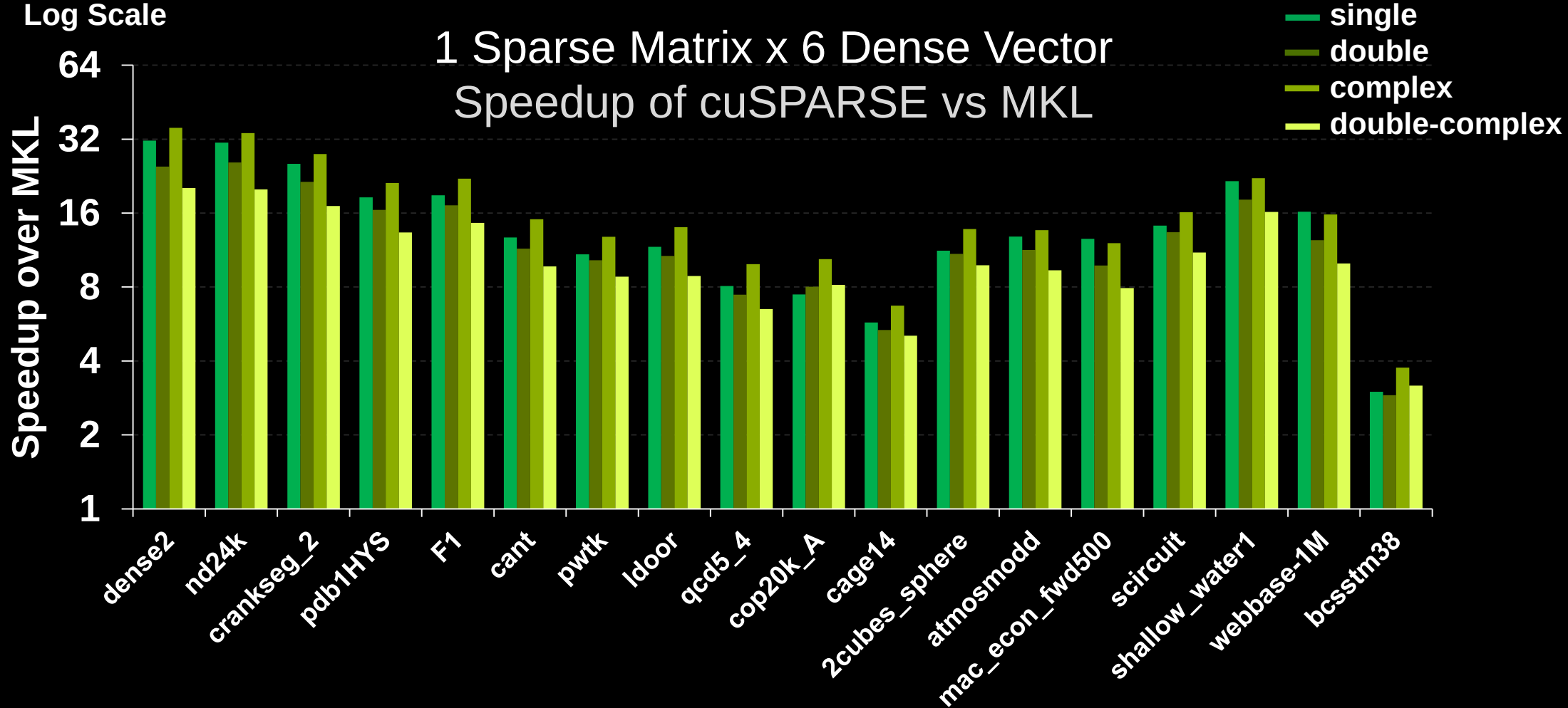
cuSPARSE

- New library for sparse linear algebra
- Conversion routines for dense, COO, CSR and CSC formats
- Optimized sparse matrix-vector multiplication

$$\begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \end{bmatrix} = \alpha \begin{bmatrix} 1.0 & & & \\ 2.0 & 3.0 & & \\ & & 4.0 & \\ 5.0 & & 6.0 & 7.0 \end{bmatrix} \begin{bmatrix} 1.0 \\ 2.0 \\ 3.0 \\ 4.0 \end{bmatrix} + \beta \begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \end{bmatrix}$$

32x Faster

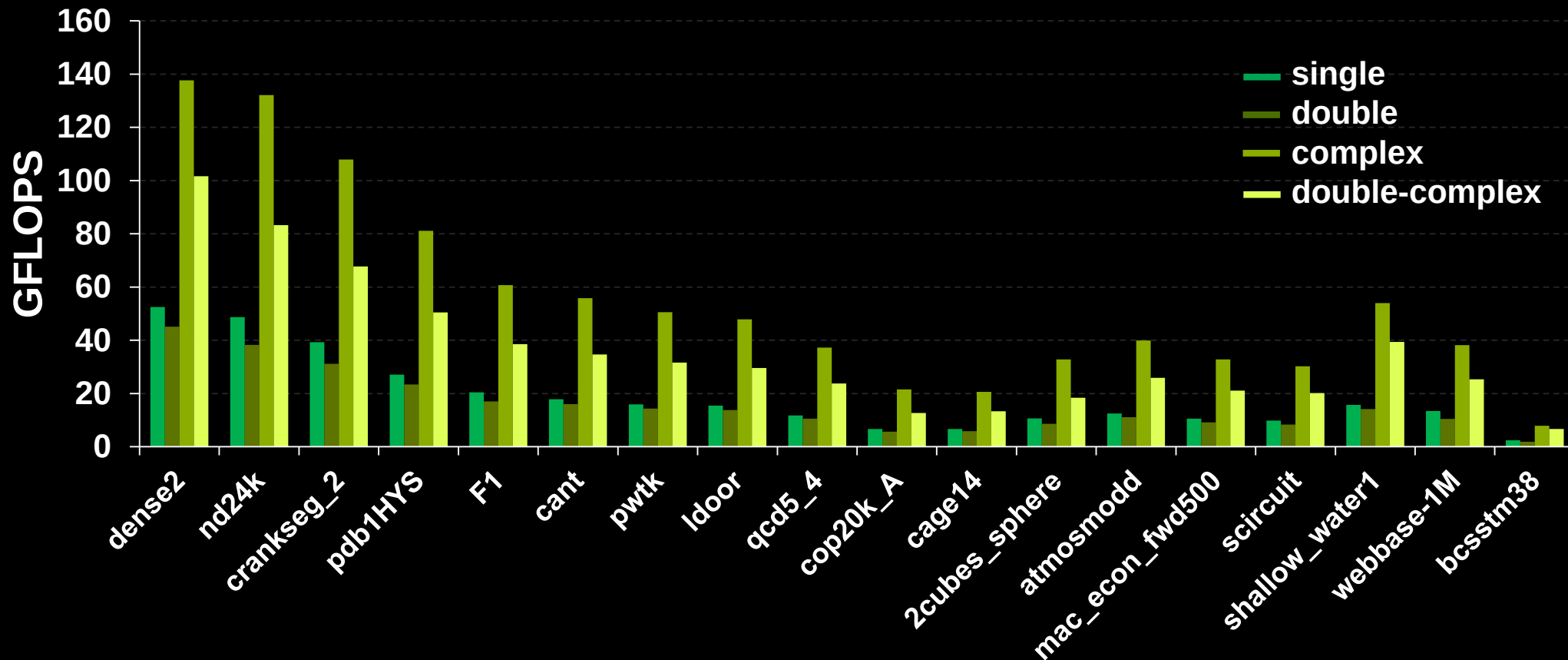
1 Sparse Matrix x 6 Dense Vector
Speedup of cuSPARSE vs MKL



* CUSPARSE 3.2, NVIDIA C2050 (Fermi), ECC on

* MKL 10.2.3, 4-core Corei7 @ 3.07GHz

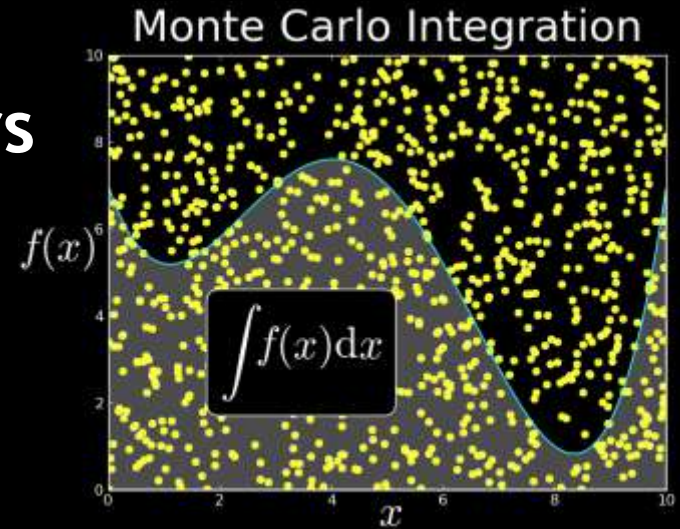
Performance of 1 Sparse Matrix x 6 Dense Vectors



Test cases roughly in order of increasing sparseness

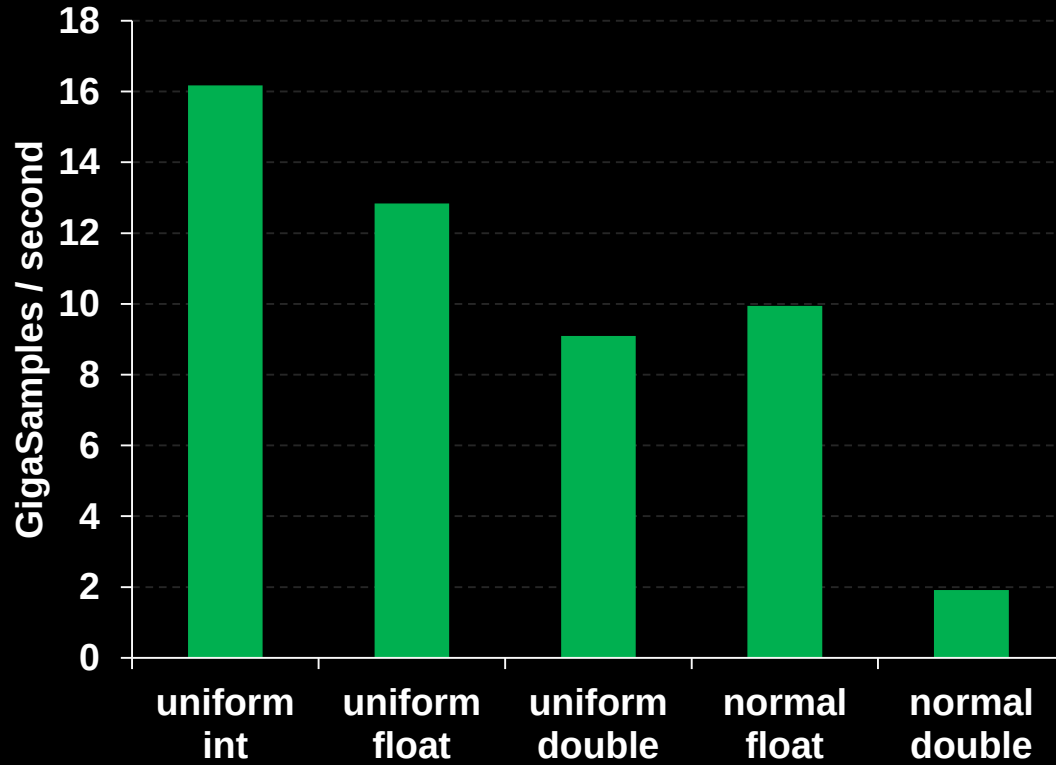
cuRAND

- Library for generating random numbers
- Features supported in CUDA 3.2
 - XORWOW pseudo-random generator
 - Sobol' quasi-random number generators
 - Host API for generating random numbers in bulk
 - Inline implementation allows use inside GPU functions/kernels
 - Single- and double-precision, uniform and normal distributions



cuRAND Performance

XORWOW Psuedo-RNG



Sobol' Quasi-RNG (1 dimension)

